### 3.1 Multiply and Divide Integers



## Multiplication $=$

$$
\text { You buy } 3 \text { tickets for } \$ 5 \text { each. How much did you spend? }
$$

Notation:

| $3(5)$ | $3(-5)$ | $-3(5)$ | $-3(-5)$ |
| :--- | :--- | :--- | :--- |

## MULTIPLICATION RULES

When multiplying if the signs are the same the product is

When multiplying if the signs are different the product is

| $(-2)(-4)$ | $-4 \times 3$ | $3 \cdot 6$ | $-4 \times 0$ | $2(-5)(-3)$ |
| :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |

## Division $=$

$$
\text { You paid } \$ 15 \text { for } 3 \text { hours tickets. How much did each ticket cost? }
$$

Notation:

| $15 \div 3$ | $\frac{-24}{4}$ | $-12 \div 3$ | $-20 \div(-4)$ |
| :---: | :---: | :---: | :---: |
| $\frac{28}{-7}$ | $9 \div 1$ | $9 \div 0$ | $\frac{4(-3)}{2}$ |

SUMMARY:


## Perform the indicated operation.

| $1.3 \times 5=$ | $2.36 \div(-12)=$ | $3 .-40 \div(-10)=$ |
| :--- | :--- | :--- |
| $4 .-6 \times 0=$ | $5 .(6)(-10)=$ | $6 .-55 \div 5=$ |
| 7. $\frac{63}{9}=$ | $8 .-6 \div(-1)=$ | $9 .(-4)(-10)=$ |
| $10.10 \times(-3)=$ | $11 . \frac{-24}{12}=$ | $12.33 \div(-3)=$ |
| $13.8 \times(-2)=$ | $14 .-21 \div(-3)=$ | $15.9 \times(-4)=$ |
| $16.3 \cdot 8=$ | $17.10(-4)=$ | $18 .-5 \times(-9)=$ |
| $19 . \frac{-40}{-5}=$ | $20.1 \div(-1)=$ | $21.12 \div(-3)=$ |

Perform the indicated operations.

| $22.3 \times 5=$ | $23.36 \div(-12)=$ | $24 .-40 \div(-10)=$ |
| :--- | :--- | :--- |
| $25 .-6 \times 0=$ | $26 .(6)(-10)=$ | $27 .-55 \div 5=$ |
|  |  |  |

## Write a multiplication expression for each situation. Answer the question.

28. Karla borrowed $\$ 5$ each from 4 different friends. How much money does Karla owe her friends altogether?

## Expression:

Answer:
29. The temperature increased $2^{\circ}$ per hour for six hours. How many degrees did the temperature raise after six hours?

Expression:
Answer:
30. Jim was deep sea diving last week. He descends 3 feet every minute. How many feet will he descend in 10 minutes?

Expression:
Answer:

## Write a division expression for each situation. Answer the question.

31. Keith borrowed a total of $\$ 30$ by borrowing the same amount of money from 5 different friends. How much money does Keith owe each friend?

Expression: Answer:
32. The temperature fell $12^{\circ}$ over 4 hours. What was the average change in temperature per hour?

Expression: Answer:
33. Max lost 24 pounds in 8 weeks on his new weight-loss plan. What was his average change in weight per week?

Expression:
Answer:
34. Juan borrowed $\$ 4$ a day until he had borrowed a total of $\$ 88$. For how many days did he borrow money?

Expression:
Answer:

1. Perform the indicated operation.

$$
-8(-3)
$$

2. Perform the indicated operations.

$$
-5(-3)(4)
$$

3. Decide whether the following expressions are equal. Support your answer!
A) $-4(6)=3(-8)$
B) $3 \cdot 10=(-6)(5)$
C) $5(-2)(2)=-4 \cdot 5$
4. Fill in the question mark with an integer to make following expressions equal. Support your answer!
A) $-3 \cdot 6=9(?)$
B) $4(-9)=? \cdot(-6)$
C) $-5(-?)=2(20)$

SPRING ROUND!!!! How fast are you???

Go to Deltamath.com for some speed rounds. Once finished, show Mr. Brust and he will sign off below. GOOD LUCK!!!

### 3.2 Multiply and Divide Fractions



## MULTIPLY FRACTIONS

> | $\frac{1}{2} \cdot \frac{7}{8}$ | $\frac{3}{5} \cdot \frac{3}{4}$ | $\left(\frac{2}{3}\right)\left(\frac{5}{2}\right)$ | $\left(\frac{2}{7}\right)\left(-\frac{3}{5}\right)$ |
| :--- | :--- | :--- | :--- |

$3 \cdot \frac{4}{5}$
MULTIPLY AN INTEGER AND A FRACTION
$6 \cdot \frac{2}{3}$
$\frac{3}{4}(-2)$


## DIVIDE FRACTIONS

$$
\begin{array}{l|l|l}
\frac{3}{4} \div \frac{7}{5} & \frac{1}{5} \div\left(\frac{3}{10}\right) & \left(-\frac{2}{3}\right) \div\left(-\frac{4}{5}\right)
\end{array}
$$

## SUMMARY:



Multiply. Reduce to simplest form if possible.

1. $\frac{3}{5} \cdot \frac{4}{3}=$
2. $\left(\frac{3}{5}\right)\left(-\frac{1}{4}\right)=$
3. $4 \cdot \frac{2}{3}=$

Divide. Reduce to simplest form if possible.
4. $\frac{3}{5} \div \frac{4}{3}=$
5. $\left(\frac{3}{5}\right) \div\left(-\frac{1}{4}\right)=$
6. $-3 \div \frac{4}{3}=$

Perform the indicated operation. Reduce to simplest form if possible.
7. $\frac{2}{5} \cdot \frac{5}{6}=$
10. $\left(-\frac{2}{5}\right) \div\left(\frac{7}{9}\right)=$
13. $\frac{1}{2} \div \frac{4}{5}=$
16. $6 \cdot\left(-\frac{4}{3}\right)=$
17. $\left(-\frac{7}{8}\right) \div\left(-\frac{5}{4}\right)=$
12. $\frac{3}{8} \cdot 5=$
15. $\frac{4}{5} \cdot \frac{2}{3}=$
18. $(-4)\left(\frac{4}{7}\right)=$

Perform the indicated operations. Reduce to simplest form if possible.
19. $\frac{3}{5} \cdot \frac{4}{3} \cdot \frac{4}{3}=$
20. $\left(\frac{3}{5}\right)\left(-\frac{1}{4}\right)(3)=$
21. $\frac{1}{2}(8)(5)=$

## Write a multiplication expression for each situation. Answer the question.

22. Mr. Brust loves $\frac{1}{4}$ pound burgers from McDonalds. He eats 6 of these burgers for dinner. How much burger did he eat?

## Expression:

Answer:
23. The temperature increased $\frac{4}{5}$ of a degree per hour for six hours. How many degrees did the temperature raise after six hours?

Expression:
Answer:
24. Jim was deep sea diving last week. He descends $\frac{3}{4}$ of a meter every minute. How many meters will he descend in 10 minutes?

Expression:
Answer:

## Write a division expression for each situation. Answer the question.

25. Mr. Brust wants to share his $\frac{1}{4}$ burger with 2 of his kids. He cuts the burger into 3 equal parts. How much burger does each person get?

Expression:
Answer:
26. The temperature fell $\frac{3}{4}$ of a degree over $\frac{2}{3}$ of an hour. What was the average change in temperature per hour?

Expression:
Answer:
27. Max lost 24 pounds in $\frac{4}{5}$ of a month on his new weight-loss plan. What was his average change in weight per month?

Expression:
Answer:

1. Perform the indicated operation.

$$
\frac{6}{7} \div \frac{5}{2}=
$$

2. Perform the indicated operation.

$$
(-4)\left(\frac{3}{5}\right)=
$$

3. Decide whether the following expressions are equal. Support your answer!
A) $\frac{7}{8} \cdot \frac{1}{3}=\frac{7}{6} \cdot \frac{1}{4}$
B) $6 \cdot \frac{1}{8}=\frac{2}{2} \div \frac{4}{3}$
C) $\frac{1}{2} \div 4=\frac{1}{3} \cdot 6$
4. Fill in the question mark with an integer to make following expressions equal. Support your answer!
A) $\frac{4}{9} \cdot \frac{?}{3}=\frac{16}{27}$
B) $5 \div\left(\frac{3}{8}\right)=\frac{?}{3}$
C) $\left(-\frac{5}{?}\right) \div\left(\frac{7}{4}\right)=-\frac{20}{21}$

## EXIT TICKET -

SPRINT ROUND!!!! How fast are you???

Go to Deltamath.com for some speed rounds. Once finished, show Mr. Brust and he will sign off below. GOOD LUCK!!!
3.3 Multiply and Divide Mixed Numbers and Decimals

## MATH 7

Write your questions here! $\longmapsto$

SUMMARY:
$3.6 \div 2$

## DIVIDE Mixed Numbers

$$
\begin{array}{l|l}
\frac{4}{5} \div\left(3 \frac{1}{2}\right) & (-3) \div\left(-2 \frac{4}{5}\right)
\end{array}
$$

## DIVIDE Decimals

$6 \div 0.5$
$4.8 \div(-0.3)$


Multiply (Mixed Numbers). Reduce to simplest form if possible.

1. $2 \frac{3}{5} \cdot \frac{2}{3}=$
2. $\left(\frac{3}{5}\right)\left(-2 \frac{1}{4}\right)=$
3. $4 \frac{1}{2} \cdot 3 \frac{1}{2}=$

Divide (Mixed Numbers). Reduce to simplest form if possible.
4. $2 \frac{3}{4} \div \frac{4}{3}=$
5. $\left(-\frac{3}{5}\right) \div\left(-3 \frac{1}{4}\right)=$
6. $-3 \frac{1}{2} \div 1 \frac{1}{3}=$

Multiply (Decimals).
7. $1.2 \cdot 5=$
8. $(3.2)(-2.4)=$
9. $4 \cdot 0.6=$

Divide (Decimals).
10. $4.5 \div 9=$
11. $(12.6) \div(-3)=$
12. $-10.25 \div 4.1=$

Perform the indicated operation. Reduce to simplest form if possible.

| 13. $2 \frac{2}{3} \cdot \frac{5}{6}=$ | 14. $(-10)(-2.5)=$ | $15 \cdot \frac{1}{2} \div 1 \frac{5}{8}=$ |
| :--- | :--- | :--- |
| 16. $\left(-3 \frac{2}{3}\right) \div(4)=$ | $17 .(18.4) \div(4)=$ | $18 \cdot \frac{3}{8} \cdot 5 \frac{1}{2}=$ |

## Write a multiplication expression for each situation. Answer the question.

22. Sandra's hair was $5 \frac{1}{3}$ inches long. Her hair dresser cut five-eighths of it off. How many inches of Sandra's hair was cut off?

## Expression:

Answer:
23. The temperature increased $2 \frac{4}{5}$ of a degree per hour for six hours. How many degrees did the temperature raise after six hours?

Expression:
Answer:
24. Jim was deep sea diving last week. He descends 1.7 of a meter every minute. How many meters will he descend in 10 minutes?

Expression:
Answer:

Write a division expression for each situation. Answer the question.
25. Mr. Brust has $2 \frac{1}{4}$ pounds of candy from Halloween. He splits the candy into 4 piles. How much does each pile weigh?

Expression:
Answer:
26. The temperature fell 9 degrees over 1.5 of an hour. What was the average change in temperature per hour?

Expression:
Answer:
27. Max lost 24 pounds in $2 \frac{1}{2}$ of a month on his new weight-loss plan. What was his average change in weight per month?

Expression:
Answer:

1. Perform the indicated operation.

$$
\frac{5}{7} \div 2 \frac{2}{3}=
$$

2. Perform the indicated operation.

$$
(-4)(3.2)=
$$

3. Decide whether the following expressions are equal. Support your answer!
A) $2 \frac{4}{5} \cdot \frac{1}{3}=2 \frac{4}{5} \div 3$
B) $6 \cdot 0.5=12.8 \div 4$
C) $\frac{3}{2} \div 4=\frac{1}{3} \cdot 1 \frac{1}{3}$

## EXIT TICKET -

Mr. Sullivan finds a geo cake recipe that serves 6 people. He needs to make a cake that serves 18 people.

## PART A

How many times bigger does Mr. Sullivan need to make the recipe?

PART B
Fill in the blanks below so that it will serve the recipe will serve 18 people.

## 6 Servings

- $21 / 4$ cups all purpose flour
- 1.5 cups sugar
- 3 teaspoons bakingpowder
- $1 / 2$ teaspoonsalt
- 1.75 cups of milk
- 2 large eggs
- 5/4 tea spoonvarilla

18 Servings
$\qquad$ cups all purpose flour
$\qquad$ cups of sugar
$\qquad$ teaspoons of bakingpowder
$\qquad$ teaspoonsalt
$\qquad$ cups of milk
$\qquad$ large eggs
$\qquad$ teaspoons vanilla

### 3.4 Rates with Complex Fractions

## Complex Fractions

$\frac{\frac{1}{4}}{\frac{2}{3}}$
$\frac{2}{3}$

$$
\frac{5}{2 \frac{1}{2}}
$$

## Rate

You bike 30 miles in 5 hours. What is your average speed?

You jog 3 miles in
$\frac{1}{3}$ hours. What is your average speed?

You walk $1 \frac{1}{3}$ miles in $\frac{2}{5}$ hours. What is your average speed?

## Proportional

The following are proportional. Find the constant of proportionality.

| Time <br> (min) | Distance <br> (meters) |
| :---: | :---: |
| $\frac{1}{3}$ | $\frac{5}{2}$ |
| $1 \frac{1}{2}$ | $11 \frac{1}{4}$ |
| $\frac{14}{15}$ | 7 |

Mr. Kelly uses $2 \frac{1}{2}$ scoops of Whey
Protein in 12 ounces of soy milk.

| Scoops <br> (\#) | Soy Milk <br> (ounces) |
| :---: | :---: |
| $2 \frac{1}{2}$ |  |
| 2 |  |
| $\frac{2}{3}$ |  |

## SUMMARY:



Divide the complex fractions. Reduce to simplest form if possible.

## 1. <br> $\frac{\frac{3}{4}}{\frac{2}{5}}$

2. 

$\frac{4}{\frac{2}{3}}$
3.
$\frac{\frac{3}{7}}{5}$

Find the rate. LABEL YOUR ANSWER!
4. It rained $2 \frac{3}{4}$ inches in 3 hours. What is the average amount of rain per hour?
5. Dustin made $3 \frac{1}{5}$ pies in $\frac{4}{5}$ of a day. What is the average amount of pies per day?
6. $2 \frac{2}{3}$ pounds of peanuts cost you 4 dollars. What is the price per pound?

The following are proportional. Find $k$ and write an equation to represent the situation.
7.

| Time <br> (min) | Distance <br> (meters) |
| :---: | :---: |
| $1 \frac{1}{2}$ | $\frac{9}{4}$ |
| 3 | $\frac{9}{2}$ |
| 5 | $7 \frac{1}{4}$ |

9. 

| Gummy Bears <br> (pound) | $\frac{1}{8}$ | $\frac{12}{5}$ | $3 \frac{1}{2}$ |
| :---: | :---: | :---: | :---: |
| Cost <br> (dollars) | $\frac{5}{24}$ | 4 | $\frac{35}{6}$ |

The following are proportional. Find k. Fill in the table and complete the sentence.
10. Caitlyn can swim 12 laps in $\frac{1}{4}$ hours. Find her average speed in laps per hour?
11. Joey packed $2 \frac{1}{4}$ boxes in $\frac{1}{4}$ hours. Find the average speed in boxes per hour.

| Time <br> (hours) | Laps <br> (\#) |
| :---: | :---: |
| $\frac{1}{4}$ |  |
| $\frac{2}{3}$ |  |

In $\frac{2}{3}$ hours, Caitlyn swims $\qquad$ laps.
12. You buy $2 \frac{3}{4}$ yards of fabric for $4 \frac{1}{2}$ dollars. Find the price per yard of fabric.

| Length <br> (yard) | Cost <br> (\$) |
| :---: | :---: |
| $2 \frac{3}{4}$ |  |
| $\frac{1}{2}$ |  |

You buy $\frac{1}{2}$ a yard of fabric for $\qquad$ dollars.
13. Sophie can read $\frac{3}{4}$ pages in $\frac{3}{5}$ minutes. Find the average speed she can read in pages per minute.

| Time <br> (min) | Pages <br> Read <br> (\#) |
| :---: | :---: |
| $\frac{3}{5}$ |  |
| $2 \frac{2}{3}$ |  |

Sophie reads $\qquad$ pages in $2 \frac{2}{3}$ minutes.

1. Divide.

2. Anna made $2 \frac{3}{5}$ cakes in $\frac{3}{4}$ of a day. What is the average amount of cakes per day?
3. Use unit rates to compare the prices of the following corn shops. Which shop has a better price? Justify!

| Kelly Corn |
| :---: |
| $8 \frac{3}{4}$ pounds |
| for |
| 7 dollars |

$$
\begin{gathered}
\frac{\text { Corey Corn }}{3 \frac{1}{8} \text { pounds }} \\
\text { for } \\
2 \frac{1}{2} \text { dollars }
\end{gathered}
$$

## EXIT TICKET -

Mr. Bean eats $\frac{3}{4}$ of a burrito every $\frac{3}{5}$ days. Mr. Bean figures that he eats 4 burritos every 5 days. Is he correct? Explain why or why not.
$\qquad$

## DATE:

$\qquad$

Perform the indicated operation. Express your answer in simplest form.


Write an expression to represent the following, then solve it!
10. Marcus has 15 Pokemon cards. His little brother has $\frac{2}{5}$ as many Pokemon cards. How many Pokemon cards does Marcus's little brother have?
11. Keri has $4 \frac{3}{5}$ feet of licorice rope. She breaks it into 3 equal parts to share. How long is each part?
12. Taylor eats $\frac{3}{4}$ of a pie $\frac{2}{3}$ of an hour. What is the average amount of pie eaten per hour?

Find $k$ (constant of proportionality). Fill in the table and complete the sentence.
13. Marquise builds 6 model airplanes in $\frac{4}{5}$ of an hour. Find the rate at which Marquise builds in airplanes per hour.

In $\frac{1}{3}$ hours, Marquise builds $\qquad$ airplanes.

| Time <br> (hours) | Airplanes <br> (\#) |
| :---: | :---: |
| $\frac{4}{5}$ |  |
| $\frac{1}{3}$ |  |

## MULTIPLE CHOICE

14. Over a period of 3 hours, the outside temperature changed an average of $-2.25^{\circ}$ Fahrenheit per hour. Which statement correctly describes the change in the temperature from the beginning to the end of the 3 hour period?
(A) The temperature decreased by 0.75 degrees Farhrenheit.
(B) The temperature increased by 0.75 degrees Fahrenheit.
(C) The temperature decreased by 6.75 degrees Fahrenheit.
(D) The temperature increased by 6.75 degrees Fahrenheit.
15. Which situation can be modeled using this expression?

$$
4 \frac{1}{2} \div \frac{1}{4}
$$

(A) Kim has $4 \frac{1}{2}$ cups of flour. She uses $\frac{1}{4}$ cup of flour for a recipe. How many cups of flour does Kim have remaining?
(B) Alex has $4 \frac{1}{2}$ pages to read for homework. So far, he has finished $\frac{1}{4}$ of his homework. How many pages has Alex read so far?
(C) Ben has a $4 \frac{1}{2}$ foot long sandwich. He cuts the sandwich into $\frac{1}{4}$ foot long pieces. How many pieces of sandwich does Ben have?
(D) Stacy has $4 \frac{1}{2}$ hours to get ready for a concert. She spends $\frac{1}{4}$ hour showering. How many hours does Stacy have remaining to get ready?

